

# ELECTRON DRIFT, DIFFUSION, AND EFFECTIVE IONIZATION COEFFICIENTS IN SF<sub>6</sub>-CHF<sub>3</sub> AND SF<sub>6</sub>-CF<sub>4</sub> MIXTURES FROM BOLTZMANN ANALYSIS

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## ABSTRACT

The electron drift velocity, electron energy distribution function and density-normalized effective ionization coefficient are calculated for SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> mixtures. Two-term, spherical harmonic expansion approximation is utilized to calculate the swarm parameters in steady-state Townsend form Boltzmann analysis. Results show that the drift velocity  $v_d$  varies feebly with SF<sub>6</sub> content. On the other hand, a strong dependence is observed in density-normalized effective ionization coefficient with SF<sub>6</sub> content, the gas mixture becomes more electronegative as the share of SF<sub>6</sub> in gas mixtures increases. The calculated value  $E/N_{cr}$  of SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> mixtures is lower than measured value of SF<sub>6</sub>-N<sub>2</sub>. The calculated density-normalized effective ionization coefficients obtained in the paper are compared with measured data from pulsed Townsend experiments. The predicted results in the numerical simulation are in agreement with the experimental results.

## 1. INTRODUCTION

Due to its outstanding electrical, physical and excellent thermal characteristics, Sulfur Hexafluoride has been widely used in the electrical industry. Whereas a major concern have emerged that SF<sub>6</sub> is supposed to be a remarkable greenhouse gas, with a global warming potential 24 000 times greater than that of CO<sub>2</sub> for a 100 year period. In order to decrease the greenhouse impact, SF<sub>6</sub> involved mixtures with less harmful fluorocarbon gases have been

therefore investigated as alternatives to be used in electric power engineering.

SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> have been identified as effective alternatives to pure SF<sub>6</sub>. Urquijo has measured of electron drift, diffusion and effective ionization coefficients in SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> gas mixtures using pulsed Townsend method[1]. The theoretical calculation based on the numerical solutions of Boltzmann equation have been widely investigated in relevant studies for SF<sub>6</sub> involved mixtures[2-4], whereas numerical analysis regarding SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> are rare.

In this paper, we calculate the electron drift velocity, and density-normalized effective ionization coefficient at various SF<sub>6</sub> content by solving Boltzmann equation with two-term expansion for a steady Townsend discharge. The critical reduced field  $E/N_{cr}$  is then determined at which ionization exactly balances attachment. In addition, reliable data of  $(\alpha - \eta)/N$  from pulsed Townsend are plotted for the sake of comparison.

## 2. RESULTS AND DISCUSSION

### 2.1 Effective ionization coefficients and electron drift velocity of pure SF<sub>6</sub>

In the paper, the results from Boltzmann analysis within two-term approximation and the data from direct experimental measurements of the density-reduced effective ionization coefficient in pure SF<sub>6</sub> are compared in Fig. 1. It can be observed that density normalized coefficient  $(\alpha - \eta)/N$  increases with increasing reduced field strength. The numerical results are in agreement with

previously published values. Thus, the possibility of utilizing a two-term Boltzmann code constitutes a great advantage especially when dealing with a large number of computations.

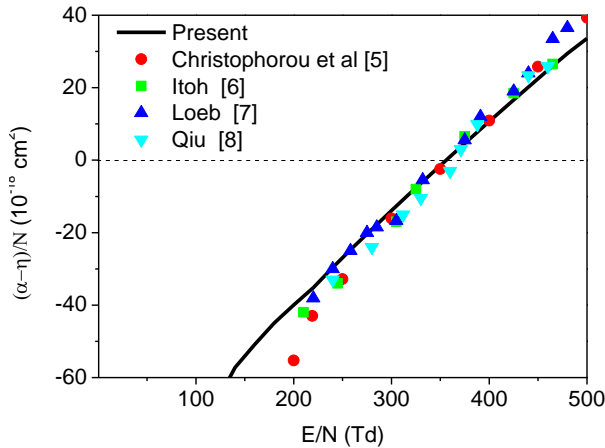


Fig. 1 Density normalized effective ionization coefficient as a function of reduced field strength at different for pure  $SF_6$

## 2.2 The electron energy distribution functions, EEDF

Fig. 2 excludes the mean electron energy as a function of  $SF_6$  content for  $SF_6$ - $CHF_3$  and  $SF_6$ - $CF_4$  mixtures when  $E/N = 200$  Td . It can be observed that mean electron energy of  $SF_6$ - $CHF_3$  mixtures decreases with increasing  $SF_6$  content. Contrarily, as the share of  $SF_6$  in  $SF_6$ - $CF_4$  mixtures increases, the corresponding mean electron energy of  $SF_6$ - $CF_4$  decreases slightly. Such discrepancies can be attributed to the variation of EEDF.

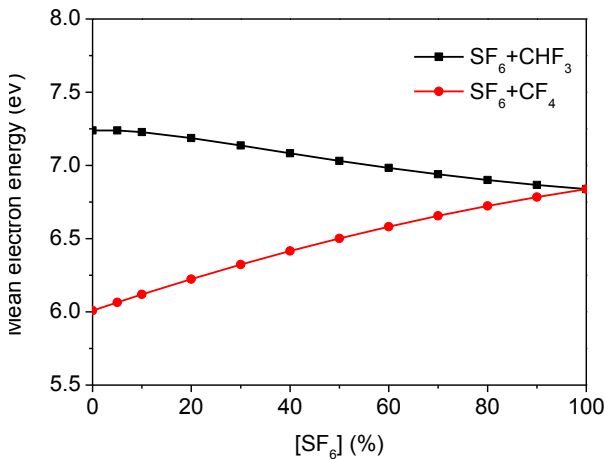


Fig.2 Mean electron energy as a function of  $SF_6$  content for  $SF_6$ - $CHF_3$  and  $SF_6$ - $CF_4$  mixtures

The addition of  $SF_6$  in  $SF_6$ - $CHF_3$  mixtures decreases the electron energy distribution function at the vicinity of the origin of energy space  $\varepsilon = 0$  as shown in Fig. 3, which leads to

the decrease of mean electron energy. With respect to  $SF_6$ - $CF_4$  mixtures, as the share of  $SF_6$  in gas mixtures increases, electron energy distribution function hardly differs near  $\varepsilon = 0$  , whereas the electron energy distribution function shifts to the right in the low electron energy region as shown in Fig. 4, which causes the mean electron energy of  $SF_6$ - $CF_4$  mixtures increases with increasing  $SF_6$  content.

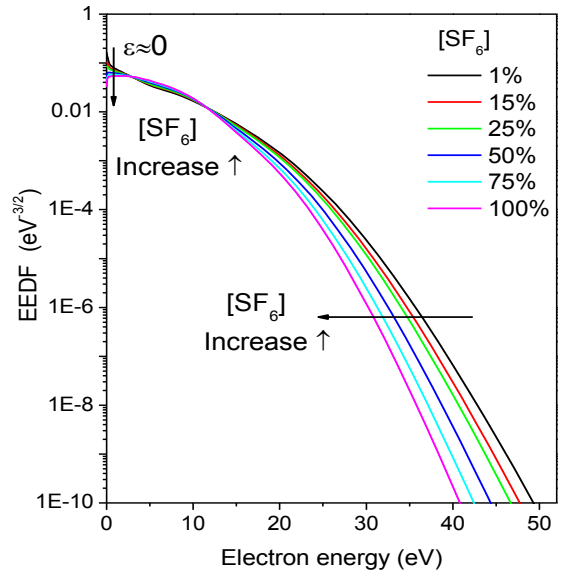


Fig. 3 Electron energy distribution functions of  $SF_6$ - $CHF_3$  mixtures

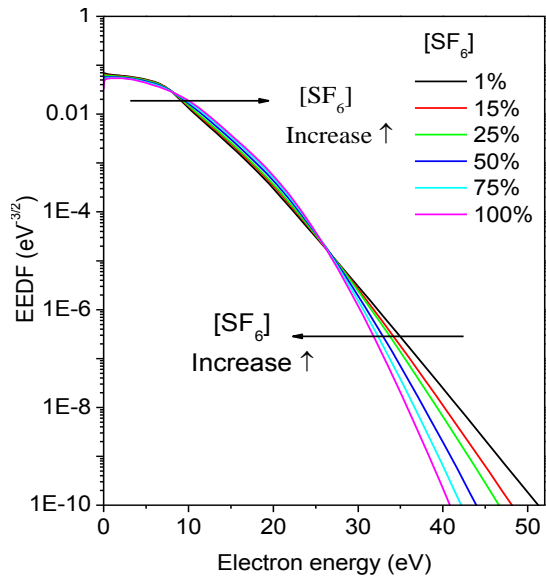


Fig. 4 Electron energy distribution functions of  $SF_6$ - $CF_4$  mixtures

## 2.3 Drift velocity

Fig. 5 and Fig. 6 describe the calculated electron drift velocity as a function of reduced field strength for  $SF_6$ - $CHF_3$  and  $SF_6$ - $CF_4$  mixtures. As it can be seen from the figures, drift velocity  $v_D$  increases with increasing reduced field strength and it varies weakly when the share of  $SF_6$  in

SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> mixtures varies from 1% to 100%, especially in the relatively high reduced field region. At a fixed reduced field strength, the drift velocity decreases gradually with increasing SF<sub>6</sub> content for SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> mixtures. The reasons for the changes in drift velocity  $v_D$  are twofold. Primarily, the effective collision frequencies for momentum transfer in SF<sub>6</sub> and CHF<sub>3</sub>/CF<sub>4</sub> weigh differently as the share of SF<sub>6</sub> in gas mixtures varies. In addition, the most important changes arise from the modifications on the EEDF as the SF<sub>6</sub> content increases. It can be also noted the interaction of electrons within the gas mixtures is strongly dominated by CHF<sub>3</sub> and CF<sub>4</sub>, especially for CHF<sub>3</sub> in SF<sub>6</sub>-CHF<sub>3</sub> mixtures, in which the electron drift velocity  $v_D$  decreases very feebly with SF<sub>6</sub> content even in the low reduced field strength  $E/N$  region due to the fact that CHF<sub>3</sub> is a highly polar molecule[5].

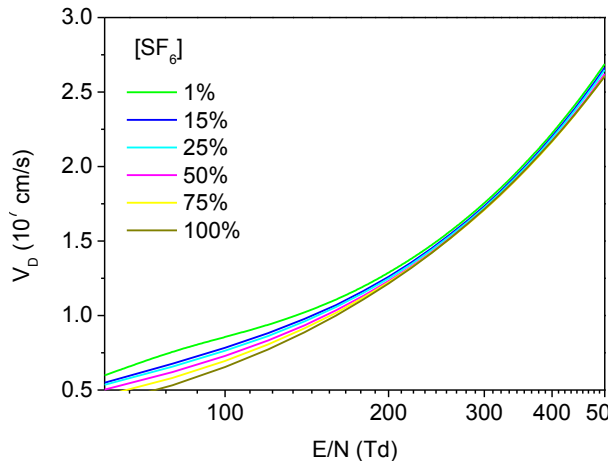


Fig. 5 Electron drift velocity as a function of reduced field strength for SF<sub>6</sub>-CHF<sub>3</sub> mixtures

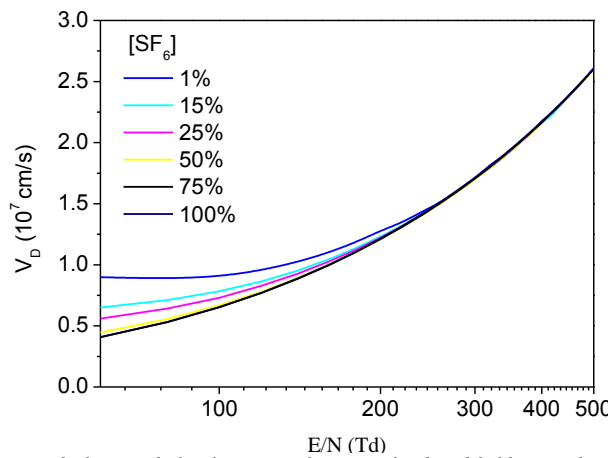


Fig. 6 Electron drift velocity as a function of reduced field strength for SF<sub>6</sub>-CF<sub>4</sub> mixtures

### 3.4 Density-normalized effective ionization coefficient and critical field strength.

The density-normalized effective ionization coefficients  $(\alpha - \eta)/N$  calculated in the paper for SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> gas mixtures with 1%, 15%, 25%, 50%, 75% and 100% as a function of reduced field strength are displayed in Fig. 7 and Fig. 8. It indicates that density-normalized effective ionization coefficient  $(\alpha - \eta)/N$  increases with increasing reduced field  $E/N$ . For a given value, it decreases as the share of CHF<sub>3</sub>/CF<sub>4</sub> content in gas mixtures decreases. This is a consequence of the increasingly electronegative character of the SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> gas mixtures. For the sake of comparison with published, reliable data are displayed as well.

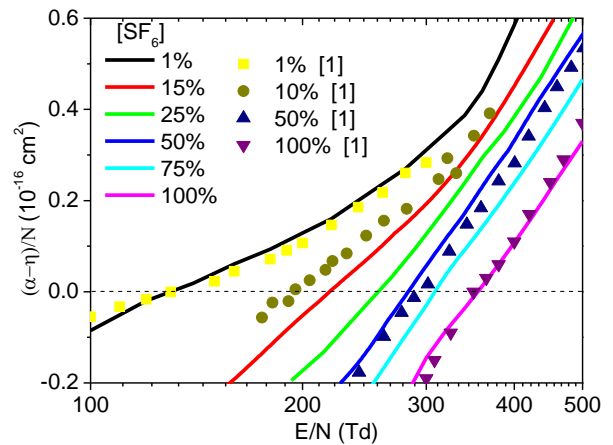


Fig. 7 The density-normalized ionization coefficient for SF<sub>6</sub>-CHF<sub>3</sub> mixtures

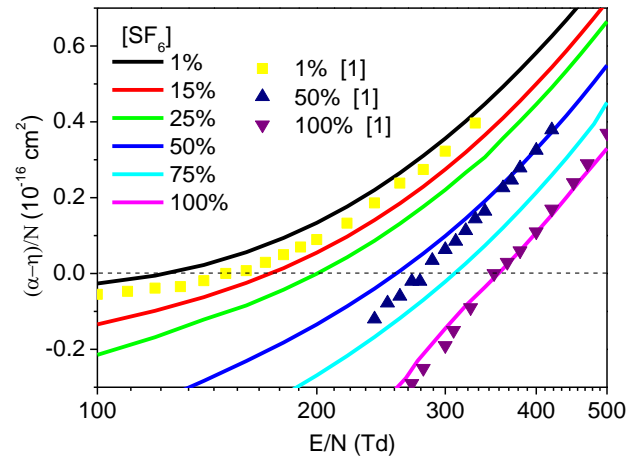


Fig. 8 The density-normalized ionization coefficient for SF<sub>6</sub>-CF<sub>4</sub> mixtures

In what concerns now the  $E/N_{cr}$ , the critical values at which ionization exactly balances attachment when  $(\alpha - \eta)/N = 0$ , as a function of

SF<sub>6</sub> content in SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> gas mixtures are plotted in Fig. 9, together with the Urquijo's experimental data and those for SF<sub>6</sub>-N<sub>2</sub> mixture for the sake of comparison, since the SF<sub>6</sub>-N<sub>2</sub> have been widely studied in relevant studies. It can be seen the critical reduced strength  $E/N_{cr}$  increases with increasing SF<sub>6</sub> content, yet the value of  $E/N_{cr}$  varies weakly between SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> gas mixtures as SF<sub>6</sub> content increases. Moreover the agreement between theory and experiment is acceptable in SF<sub>6</sub>-CHF<sub>3</sub> and fair in SF<sub>6</sub>-CF<sub>4</sub> although some discrepancies are observed as the share of SF<sub>6</sub> in gas mixtures increases. The overall calculated values  $E/N_{cr}$  in SF<sub>6</sub>-CHF<sub>3</sub> are higher than the measured data while the critical values are lower than the measured data in SF<sub>6</sub>-CF<sub>4</sub> mixtures with SF<sub>6</sub> content variation. Now that the  $E/N_{cr}$  values in SF<sub>6</sub>-N<sub>2</sub> are consistently higher than those in SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> gas mixtures as indicated by [9], the critical values are by far larger in SF<sub>6</sub>-N<sub>2</sub> than in other SF<sub>6</sub> involved gas mixtures, due to the relatively low ionization rate coefficients in N<sub>2</sub> and the influence of N<sub>2</sub> as a good electron scattered that performs in the overall attachment process.

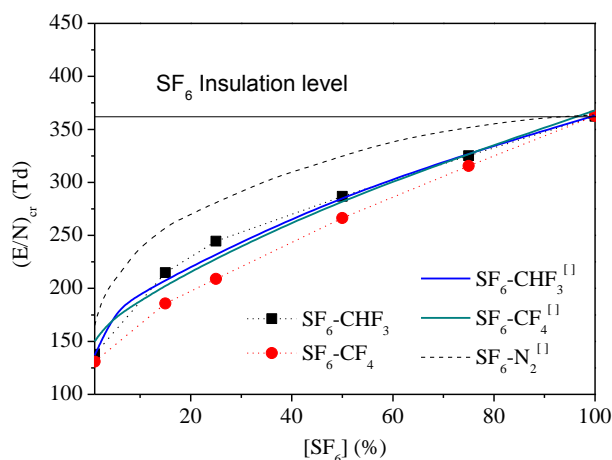


Fig. 9 The critical reduced field strength as a function of SF<sub>6</sub> content

### 3. CONCLUSION

In this paper, density normalized effective ionization coefficients, electron energy distribution function and electron drift velocity for are all calculated using Boltzmann equation along with two-term approximation for SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> mixtures. The critical electric field strength  $E/N_{cr}$ , at which the ionization and attachment rate are exactly balanced, is determined for SF<sub>6</sub>-CHF<sub>3</sub> and SF<sub>6</sub>-CF<sub>4</sub> mixtures

as a function of SF<sub>6</sub> content. By comparing with the previous published values, two-term expansion is confirmed to be a valid approach.

### ACKNOWLEDGEMENT

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